

Numbers – Sets & Properties

Exploring Real Number Sets: Define each number set based on the number examples given.

Natural Numbers: 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12...



the counting numbers

Whole Numbers: 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12...



the Natural #'s and zero

Integers: ...-6, -5, -4, -3, -2, -1, 0, 1, 2, 3, 4, 5, 6...

the whole numbers and their opposites.

Rational Numbers: $\frac{1}{2}, \frac{3}{4}, \frac{-2}{5}, \frac{9}{3}, \frac{-7}{7}, \frac{0}{8}, \dots$

Fractions ... numbers of the form $\frac{a}{b}$ where a and b are integers.

Irrational Numbers: $\pi, \sqrt{2}, -\sqrt{3}, \sqrt{7}, \dots$

that can't be written as $\frac{a}{b}$, where a and b are integers.

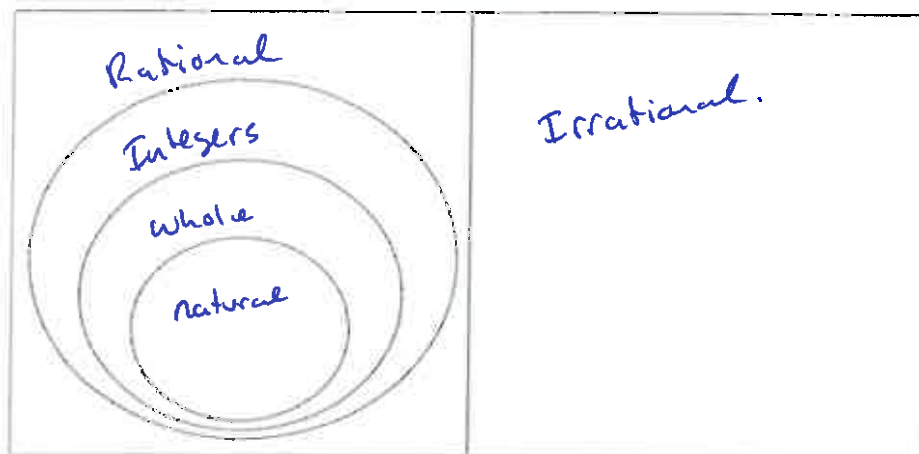
Real Numbers: $0, \pm 1, \pm 2, \pm\sqrt{2}, \pm\frac{5}{7}, \pm\frac{9}{3}, \dots$



Rational and irrational # put together.

Write each number set in its appropriate place on the Venn diagram:

Real Numbers





Exploring Closure: What does it mean for a set of numbers to be "Closed"?

Using an operation to combine 2 numbers from a set results in a number in the same set.

For each operation, if the number set is closed, explain why. If the set is not closed, give a counterexample.

Number Set	Addition	Subtraction	Multiplication	Division
Natural Numbers 	Closed. Adding 2 natural #'s makes a natural #.	closed	closed	not closed $\frac{1}{2}$ is not not natural.
Whole Numbers 	closed	closed	closed	$\frac{1}{2}$ is not not closed whole
Integers	closed	closed	closed	$\frac{1}{2}$ not is not closed integer
Rational Numbers	closed	closed	closed	Closed $\frac{1}{2}$ is rational.
Irrational Numbers	closed	closed	not closed: $\sqrt{2} \cdot \sqrt{2} = \sqrt{4}$ $= 2$ Is not irrational.	not closed $\frac{\sqrt{2}}{\sqrt{2}} = 1$ not irrational.
Real Numbers 	closed	closed	closed	closed.



Number Properties:

1. Commutative Property:

Addition: $a + b = \underline{b + a}$

Multiplication: $ab = \underline{ba}$

2. Associative Property:

Addition: $(a + b) + c = \underline{a + (b + c)}$

Multiplication: $(ab)c = \underline{a(bc)}$

3. Identity Property:

Addition: $a + 0 = \underline{a}$

Multiplication: $a \cdot 1 = \underline{a}$

4. Inverse Property:

Addition: $a + -a = \underline{0}$

Multiplication: $a \cdot \frac{1}{a} = \underline{1}$

5. Distributive Property:

Addition: $a(b + c) = \underline{ab + ac}$

Subtraction: $a(b - c) = \underline{ab - ac}$



Examples

1. Name the property that each illustrates.

a. $9 + 7 = 7 + 9$

Commutative. (x)

b. $(8 \cdot 4) \cdot 3 = 8 \cdot (4 \cdot 3)$

Associative. (+)

c. $3 + 0 = 3$

Identity of addition.

d. $np = pn$

Commutative. (x)

2. Next to each step, identify the property used in the step.

$8(x + 4) + 2x$

$8x + 32 + 2x$

distributive property

$32 + 8x + 2x$

Commutative.

$32 + 10x$

combine like terms.

